# POWER LOSSES IN RF INDUCTOR OF FERRITE-FREE CLOSED-LOOP INDUCTIVELY-COUPLED LOW PRESSURE MERCURY LAMPS

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### ABSTRACT

RF inductor power losses of ferrite-free electrode-less low pressure mercury inductively-coupled discharges excited in closed-loop dielectric tube were studied. The modelling was made within the framework of low pressure inductive discharge transformer model for discharge lamps with tubes of 16, 25 and 38 mm inner diam. filled with the mixture of mercury vapour  $(7.5 \times 10^{-3} \text{ mm Hg})$ and argon (0.1, 0.3 and 1.0 mm Hg) at RF frequencies of 1, 7; 3.4 and 5.1 MHz and plasma power of (25-500) W. Discharges were excited with the help of the induction coil of 3, 4 and 6 turns placed along the inner perimeter of the closed-loop tube. It was found that the dependence of coil power losses,  $P_{\text{coil}}$ , on the discharge plasma power,  $P_{\text{pl}}$ , had the minimum while  $P_{coil}$  decreased with RF frequency, tube diameter and coil number of turns. The modelling results were found in good qualitative agreement with the experimental data; quantitative discrepancies are believed to be due skin-effect and RF electric field radial inhomogeneity that were not included in discharge modelling.

**Keywords**: inductively-coupled discharge, closed-loop tube, low pressure mercury plasma, induction coil power losses

### **1. INTRODUCTION**

Plasma of ferrite-free inductively-coupled discharges excited in mixture of low pressure (LP) mercury vapour and inert gases in closed-loop quartz tubes are considered as perspectives high efficient sources of UV radiation [1, 2]. Due to the absence of internal electrodes, electrode-less mercury UV lamps can operate at low buffer inert gas pressures of (0.1-0.5) mm Hg that provides maximum efficiency of resonant UV radiation [3].

Since electromagnetic radiation at frequencies of f < 10MHz is negligible [4], lamp RF power  $P_{\text{lamp}}$  is a sum of power absorbed by discharge plasma,  $P_{\text{pl}}$ , and power losses in coil wire,  $P_{\text{coil}}$  [5, 6]. Thus, to increase UV lamp efficiency one has to increase coil power efficiency  $\eta_{\text{coil}} = (1 - P_{\text{coil}}/P_{\text{lamp}})$  [1], i.e. to minimise  $P_{\text{coil}}$ .

In the present work, effects of lamp parameters (discharge tube diameter, inert gas pressure, number of coil turns, N, operation frequency, f, and plasma absorbed power,  $P_{pl}$ ) on coil power losses,  $P_{coil}$ , were theoretically studied with the help of transformer model of LP induction discharge [5, 6].

### 2. DISCHARGE TUBE AND RF INDUCTOR

The lamps studied had length  $(l_{\text{lamp}})$  of 406, 426 and 454 mm and width  $(H_{\text{lamp}})$  of 106, 126 and 154 mm, respectively. Discharge tube had inner diameter  $(d_t)$  of 16, 25 and 38mm and wall thickness ( $\Delta$ ) of 1.0, 1.5 and 2.0 mm, respectively. Induction coils of 3, 4 and 6 turns were made from multiple strand copper wire (Litz wire) with diameter  $(d_w)$  of 1.63 mm and resistance per unit length  $(\rho_w)$  of 8.5×10<sup>-4</sup> Ω/cm (at f = (2-5) MHz). The coil turns were placed along the inner perimeter of the lamp that had "long"  $(l_{per})$  length and "short"  $(H_{per})$ length of 370 and 70 mm, respectively (Fig. 1).



Fig. 1. Diagram of ferrite-free electrode-less inductively-coupled lamp with a closedloop discharge tube and RF inductor (coil)

Mercury vapour pressure was  $7.5 \times 10^{-3}$  mm Hg (maximum UV radiation flux), inert gas (argon) pressures – 0.1, 0.3 and 1.0 mm Hg. Operation frequencies *f* are equal to (1,7–5,1) MHz, were chosen to satisfy condition  $\omega \ll v_e$  (where  $\omega = 2\pi f$  is the circular frequency of RF field,  $v_e$  is the frequency of elastic collisions of electrons with mercury and argon atoms) that allows us to neglect the inductive component of plasma RF electric field. All calculation had been done at plasma powers  $P_{\rm pl}$  in range (25–500) W.

# 3. PLASMA AND COIL PARAMETERS EQUATIONS

For calculation of plasma and coil electric parameters, the transformer model of LP induction discharge [5, 6] was used with assumptions of direct-current analogy [4] and RF electric field,  $E_{\rm pl}$ , spatial (radial and azimuth) uniformity, and neglecting of skin-effect.

 $P_{\rm coil}$  was calculated as

$$P_{\rm coil} = I_{\rm coil}^2 R_{\rm coil},\tag{1}$$

where  $I_{coil}$  is the RF current in the induction coil and  $R_{coil}$  is coil resistance calculated as

$$R_{\rm coil} = \rho_{\rm w} l_{\rm coil}, \qquad (2)$$

where  $l_{coil}$  is the length of coil wire defined as

$$l_{\rm coil} = 2(l_{\rm per} + H_{\rm per})N.$$
(3)

In accordance with the transformer model of induction discharge, the expression for inductor RF current,  $I_{coil}$ , has the following expression [6]

$$I_{\rm coil} = \frac{\bar{E}_{\rm pl} \Lambda_{\rm pl} \sqrt{1 + Q_{\rm pl}^2}}{\omega M} , \qquad (4)$$

where  $\Lambda_{pl}$  is the length of plasma turn defined as length of centre line of the closed discharge tube,  $\bar{E}_{pl}$  is the active component of plasma electric field averaged over cross-section of plasma turn, M is the mutual inductance of the plasma turn and the induction coil [5, 6]:

$$M = k \sqrt{L_{\rm coil} L_{\rm ind}} , \qquad (5)$$

where  $L_{\text{coil}}$  is the inductance of disc shape induction coil  $(D_{\text{coil}} >> H_{\text{coil}})$ :

$$L_{\rm coil} = 0,56\mu_{\rm o}\pi D_{\rm coil}N^2 \tag{6},$$

where  $H_{\text{coil}} \approx d_{\text{w}}$  is the coil height,  $D_{\text{coil}} = (4S_{\text{coil}}/\pi)^{1/2}$  is the coil equivalent diameter; *k* is the coupling coefficient of the plasma turn and the induction coil calculated as the ratio of the area encircled by the coil turn  $S_{\text{coil}}$  to the area encircled by the plasma turn  $S_{\text{pl}}$  [5, 6]:

$$k = \frac{S_{\text{coil}}}{S_{\text{pl}}},$$

where  $Q_{\rm pl}$  is the plasma turn quality-factor that is defined as

$$Q_{\rm pl} = \frac{\omega L_{\rm ind}}{R_{\rm pl}},$$

where  $R_{\rm pl} = P_{\rm pl}/I_{\rm pl}^2$  is the plasma turn resistance,  $I_{\rm pl}$  *is* the discharge current,  $L_{\rm ind}$  is the geometric inductance of plasma turn [7]:

$$L_{\rm ind} = 2\pi D_{\rm pl} \left[ \ln \left( \frac{4D_{\rm pl}}{0.39d_{\rm pl}} \right) - 2 \right] \cdot 10^{-9},$$

where  $d_{\rm pl} \approx 0.75 d_{\rm t}$  is the diameter of cross-section of plasma turn,  $D_{\rm pl} = (4S_{\rm pl}/\pi)^{1/2}$  is the equivalent diameter of the area encircled by plasma turn,  $S_{\rm pl}$  [8].



Fig. 2. Dependence of coil power losses,  $P_{\text{coil}}$ , on plasma power  $P_{\text{pl}}$ , tube diameter  $d_t$ , mm: 16 (red), 25 (blue), 38 (black); argon pressure  $p_{\text{AP}}$  mmHg:  $\bullet - 0.1$ ;  $\blacktriangle - 0.3$ ;  $\blacksquare -$ 1.0; number of coil turns N = 4; RF frequency f = 3.4MHz

The equation that connects coil power losses,  $P_{\text{coil}}$ , with induction coil and discharge plasma parameters could be obtained from (1, 4):

$$P_{\rm coil} = \frac{\left(\bar{E}_{\rm pl}\Lambda_{\rm pl}\right)^2 (1+Q_{\rm pl}^2)\rho_{\rm w} l_{\rm coil}}{\left(\omega M\right)^2} \ . \tag{7}$$

And using (3), (5), (6) and (7) one can get an expression that could be used for  $P_{\text{coil}}$  calculation:

$$P_{\text{coil}} = \frac{\left(\bar{E}_{\text{pl}}A_{\text{pl}}\right)^{2}(1+Q_{\text{pl}}^{2})\rho_{\text{w}}(l_{\text{per}}+H_{\text{per}})}{0,28\mu_{\text{o}}\pi D_{\text{coil}}N(k\omega)^{2}L_{\text{ind}}}.$$
(8)

With the approximation of direct-current analogy, we used values of electric field,  $E_{pl}$ , in the plasma positive column of argon-mercury discharge with the same tube diameter and fill pressure and operated at the same plasma power but at low frequency of 50 Hz [9].

# 4. CALCULATIONS RESULTS AND DISCUSSION

The dependencies of  $P_{coil}$  on  $P_{pl}$  calculated for lamps with various discharge tube and RF inductor parameters are shown in Fig. 2–5. It is seen that at relatively low values of  $P_{pl}$  values of  $P_{coil}$  in all



Fig. 3. Dependence of  $P_{coil}$  on  $P_{pl}$ ,  $d_t$ , mm: 16 (red), 25 (blue), 38 (black);  $p_{Ar}$ , mmHg:  $\bullet - 0.1$ ;  $\blacktriangle - 0.3$ ;  $\blacksquare - 1.0$ ; N = 4; f = 5.1MHz

lamps decrease considerably with  $P_{pl}$  increase. As  $P_{pl}$  grows the decrease of  $P_{coil}$  "slows down" and at a certain plasma power value,  $P_{pl} = P_{pl, min}$ , coil power losses reach their minimum value,  $P_{coil, min}$ , and then slightly increases with  $P_{pl}$ . The larger tube diameter,  $d_t$ , the lower value of  $P_{pl, min}$  at which coil power losses reach their minimum value,  $P_{coil, min}$ .

The increase of RF frequency f causes the decrease of  $P_{\rm coil}$  and shifts value of  $P_{\rm pl, min}$  to smaller values of  $P_{\rm pl}$ . The effect of RF frequency on coil power losses can be explained by the transformer model of induction discharge excited at RF frequencies,  $\omega \ll v_{\rm e}$ , which do not affect plasma power balance [4]. Therefore,  $\bar{E}_{\rm pl}$  and, hence, plasma turn RF voltage,  $U_{\rm pl}$  (=  $\bar{E}_{\rm pl}A_{\rm pl}$ ), do not depend from RF frequency  $\omega$ . Note that in accordance with the induction discharge transformer model, coil RF voltage,  $U_{\rm coil}$ , is related to  $U_{\rm pl}$  as  $U_{\rm coil} \approx U_{\rm pl}N/k^{1/2}$  [2, 6].

At the same time, coil inductive resistance,  $\omega L_{coil}$  (here  $L_{coil}$  is coil conductance), increases linearly with the increase of RF frequency,  $\omega = 2\pi f$ . Since coil inductive resistance,  $\omega L_{coil} >> R_{coil}$ , the induction coil impedance has inductive character so RF coil current,  $I_{coil}$ , could be determined as,  $I_{coil} \approx$   $U_{coil}/(\omega L_{coil})$ . Thus,  $I_{coil}$  is inversely proportional to  $\omega$  while coil power losses,  $P_{coil} \sim I_{coil}^2$  (see Eq. (1)) are inversely proportional to  $f^2$ . This is justified by the results of calculation of  $P_{coil}$  made at two RF frequencies, f = 3,4 and 5,1 MHz, for induction lamps with identical lamp parameters (Figs. 2,3).



Fig. 4. Dependence of  $P_{coil}$  on  $P_{pl}$ ;  $d_t = 25$ mm; N: 3 (red), 4 (blue), 6 (black);  $p_{Ar}$ , mmHg:  $\bullet - 0.1$ ;  $\blacktriangle - 0.3$ ;  $\blacksquare - 1.0$ ; f = 3.4MHz

It can be also seen from Figs. 2 and 3 that at relatively high values of  $P_{pl}$  in the lamp with  $d_t = 38$  mm,  $P_{coil}$  could be higher than that in the lamp with  $d_t = 25$ mm. The higher *f*, the lower value of  $P_{pl}$  at which the curves  $P_{coil}$  ( $P_{pl}$ ) calculated for lamps with different diameter "cross".

In low temperature low pressure (LP) plasmas, the increase of plasma power (actually, plasma electron density,  $n_e$ ) causes the transition of ionization mechanism from electron-atom single collision to two-step ionisation process and, hence, to reduction of RF electric field in plasma,  $E_{pl}$  [4]. In non-ferrite LP induction discharges excited with the help of induction coil at frequencies of  $\omega \ll v_e$ , lowering of  $\bar{E}_{pl}$  causes in accordance with (7) and (8) the decrease of  $P_{coil}$ .

Reducing lamp tube diameter,  $d_t$ , from 16 mm to 25mm leads to the decrease of plasma electric field,  $\bar{E}_{pl}$ , [2, 9] that in its turn causes significantly, in accordance with (8), decrease coil power losses,  $P_{coil}$  (Figs. 2 and 3) and k (due to the increase of  $S_{pl}$ ) but results in the increase of  $\Lambda_{pl}$  and  $Q_{pl}$ . As it follows from (8) and is shown in Figs. 2 and 3, the dependence of  $P_{coil}$  on  $d_t$  turn out to be very complex and has its minimum at relatively high values of  $P_{pl}$  and f.

Increase of buffer gas (argon) pressure from 0.1 to 1.0 mmHg causes insignificant decrease of  $E_{pl}$  [9] and, in accordance with (7) and (8), slight decrease of  $P_{coil}$  (Figs. 2 and 3).



Fig. 5. Dependence of  $P_{coil}$  on  $P_{pl}$ ;  $d_t = 16$ mm and 25mm;  $p_{Ar} = 1.0$ mmHg; N = 3; f = 1.7MHz

Increase of  $P_{pl}$  (and, therefore,  $I_{pl}$  and  $n_e$ ) is accompanied by the decrease of  $R_{\rm pl}$ , that (with a reasonable assumption of independence of  $L_{ind}$  on  $I_{pl}$ ) causes the growth of plasma quality factor,  $Q_{\rm pl}$  (=  $\omega L_{\rm ind}/R_{\rm pl}$ ). At low values of  $P_{\rm pl}$ , when  $R_{\rm pl}$  is high, plasma quality factor,  $Q_{pl}$ , is very low (<0.1) and in accordance with (7) and (8) does not affect  $P_{\text{coil}}$ . The further increase of  $P_{\text{pl}}$  and  $d_{\text{t}}$  causes the decrease of  $R_{pl}$  and, hence, the growth of  $Q_{pl}$  that increasingly affects  $P_{coil}$  and the character of the dependence of  $P_{coil}$  on  $P_{pl}$  that changes from "negative" to positive" one forming the minimum at  $P_{\rm pl, min}$  (Fig. 3). Similar dependences of  $P_{\rm coil}$  on  $P_{\rm pl}$ , with the their minimums shifted with increase of fand  $d_{\rm t}$  to lower values of  $P_{\rm pl}$ , were experimentally observed in linear ferrite-free electrode-less lamps excited with the help of induction coil at f = 6-12MHz [10].

The effect of the number of coil turns, N, on coil power losses,  $P_{\text{coil}}$ , is shown in Fig. 4. It is seen that in accordance with (8),  $P_{\text{coil}}$  is inversely proportional to N.

## 5. COMPARISON OF CALCULATION RESULTS WITH THE EXPERIMENT

The experimental data of  $P_{coil}$  measured in two inductive lamps with tube diameter 16 and 25 mm excited at RF frequency of 1,7 MHz are presented in Fig. 5 as functions of  $P_{pl}$ . The dependencies of  $P_{coil}$ on  $P_{pl}$  calculated for the same lamps are plotted in Fig. 5. It is seen that the experimental dependence



Fig. 6. Dependence of RF inductor (coil) power efficiency,  $\eta_{\text{coil}}$ , on  $P_{\text{pl}}$ .  $d_{\text{t}} = 16$  mm and 25 mm;  $p_{\text{Ar}} = 1.0$  mmHg; N = 3; f = 1.7MHz

of  $P_{\text{coil}}$  on  $P_{\text{pl}}$  of the lamp with smaller tube diameter (16 mm) has shallow minimum at  $P_{\text{pl}, \min} = 60$ W while the experimental dependence of  $P_{\text{coil}}$  on  $P_{\text{pl}}$ of the lamp with larger tube diameter (25 mm) has deep minimum at  $P_{\text{pl}, \min} = 85$ W. It should be noted that the calculated values of  $P_{\text{coil}}$  of the lamp with  $d_t = 16$  mm are in good agreement with the calculated data of  $P_{\text{coil}}$  of the lamp with the tube of larger diameter (25 mm) considerably exceed the experimental ones at  $P_{\text{pl}, \min} > 90$  W.

It is from Fig. 5 that both minimums in dependencies  $P_{coil}(P_{pl})$  are at plasma powers,  $P_{pl, min}$ , which are much smaller than those caused by coil power losses increase due to the growth of plasma quality factor,  $Q_{pl} > 0,3$ , see (8). It is believed that the minimums in Fig. 5 and further growth of  $P_{coil}$ observed in the experimental dependencies of  $P_{coil}$ on  $P_{pl}$  are related to skin effect pronounced in induction discharges at f = 1-5MHz and plasma densities,  $n_e > 10^{11}$ cm<sup>-3</sup> [4, 10, 11].

Indeed, skin effect that "pushes" RF electric field to discharge tube walls where coil wire is located, thereby, increases  $\bar{E}_{pl}$  [4, 11] and thus causes the increase  $P_{coil}$ . The observed discrepancy between calculated and experimental data seems to be caused by not taking into account skin effect in inductive discharge model.

It could be seen in Fig. 6 that in both lamps, at relatively low values of  $P_{\rm pl}$ ,  $\eta_{\rm coil}$  rapidly increases with  $P_{\rm pl}$  and at high values of  $P_{\rm pl}$  asymptotically approaches to 1. The discrepancy between experimental and calculated dependencies of  $\eta_{\rm coil}$  on  $P_{\rm pl}$  in the

lamp with  $d_t = 25$ mm observed at  $P_{pl} > 85$ W are believed to be due to non-considering skin effect in LP inductive discharge model.

#### 6. CONCLUSION

• With the use of the transformer model, the analytic expression for induction coil power losses,  $P_{\text{coil}}$ , in LP inductively-coupled discharges excited at frequencies of  $\omega \ll v_{\text{e}}$  in ferrite-free closed-loop tube with the mixture of mercury vapour and argon were derived.

• It was found that the dependence of  $P_{coil}$  on plasma power,  $P_{pl}$ , has the minimum that shifts to lower values of  $P_{pl}$  as the discharge tube diameter,  $d_t$ , and RF frequency, f, increase.

• It was shown that discharge tube diameter,  $d_{\rm t}$ , affects coil power losses,  $P_{\rm coil}$ , via RF electric field, plasma turn length,  $\Lambda_{\rm pl}$ , and quality factor,  $Q_{\rm pl}$ , and plasma turn and induction coil coupling coefficient, k.

• It is found that  $P_{\text{coil}}$  is inversely proportional to coil turns number, N, and slightly decreases as argon pressures grows from 0.1 mm Hg to 1.0 mm Hg.

• The results of calculation of coil power losses,  $P_{\text{coil}}$ , and coil power efficiency,  $Q_{\text{coil}}$ , made for the ferrite-free electrode-less lamp with discharge tube diameter,  $d_t = 16$ mm, were found in satisfactory qualitative agreement with the experiment. Discrepancy between calculated and experimental obtained  $P_{\text{coil}}$  and  $Q_{\text{coil}}$  in lamp with tube diameter of 25mm at  $P_{\text{pl}} \ge 80$ W is supposedly due to not taking into account skin effect in the transformer model of LP inductively-coupled discharge.

• The results obtained could be used for optimisation of RF frequency, induction coil number of turns, and length, and diameter of discharge closedloop tube of ferrite-free electrode-less LP mercury UV lamps.

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